

GATE Aerospace 2016

Total Marks: 100

Time: 3 Hrs

Instructions:

1. This question paper consists of 2 sections, General Aptitude (GA) for 15 marks and the subject specific GATE paper for 85 marks. Both these sections are compulsory.
2. The GA section consists of 10 questions. Question numbers 1 to 5 are of 1-mark each, while question numbers 6 to 10 are of 2-mark each.
3. The subject specific GATE paper section consists of 55 questions, out of which question numbers 11 to 35 are of 1-mark each, while question numbers 36 to 65 are of 2-mark each.
4. The question paper may consist of questions of multiple choice type (MCQ) and numerical answer type.
5. Multiple choice type questions will have four choices against A, B, C, D, out of which only ONE is the correct answer.
6. For numerical answer type questions, each question will have a numerical answer and there will not be any choices.
7. All questions that are not attempted will result in zero marks. However, wrong answers for multiple choice type questions (MCQ) will result in NEGATIVE marks. For all MCQ questions a wrong answer will result in deduction of $\frac{1}{3}$ marks for a 1-mark question and $\frac{2}{3}$ marks for a 2-mark question.
8. There is NO NEGATIVE MARKING for questions of NUMERICAL ANSWER TYPE.

SECTION I: General Aptitude (GA) Questions

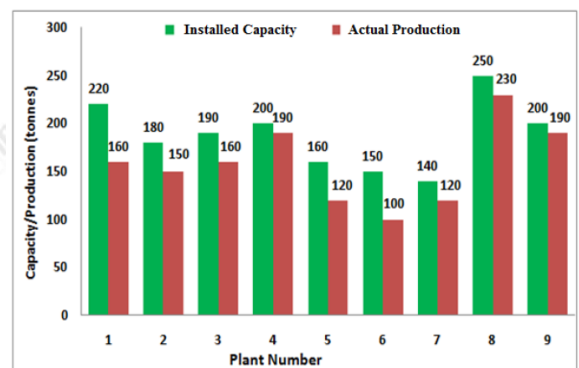
Q. 1 – Q. 5 carry one mark each.

1. The chairman requested the aggrieved shareholders to _____ him.
 (A) bare with (B) bore with
 (C) bear with (D) bare
2. Identify the correct spelling out of the given options:
 (A) Managable (B) Manageable
 (C) Mangaable (D) Managible
3. Pick the odd one out in the following:
 13, 23, 33, 43, 53
 (A) 23 (B) 33
 (C) 43 (D) 53
4. R2D2 is a robot. R2D2 can repair aeroplanes. No other robot can repair aeroplanes.
 Which of the following can be logically inferred from the above statements?
 (A) R2D2 is a robot which can only repair aeroplanes.
 (B) R2D2 is the only robot which can repair aeroplanes.
 (C) R2D2 is a robot which can repair only aeroplanes.
 (D) Only R2D2 is a robot.
5. If $|9y-6|=3$, then $y^2-4y/3$ is
 (A) 0 (B) $+1/3$
 (C) $-1/3$ (D) undefined

Q. 6 – Q. 10 carry two marks each.

6. The following graph represents the installed capacity for cement production (in tonnes) and the actual production (in tonnes) of nine cement plants of a cement company. Capacity utilization of a plant is defined as ratio of actual production of cement to installed capacity. A plant with installed capacity of at least 200 tonnes is called a large plant and a plant with

lesser capacity is called a small plant. The difference between total production of large plants and small plants, in tonnes is _____.



7. A poll of students appearing for masters in engineering indicated that 60 % of the students believed that mechanical engineering is a profession unsuitable for women. A research study on women with masters or higher degrees in mechanical engineering found that 99 % of such women were successful in their professions.

Which of the following can be logically inferred from the above paragraph?

- (A) Many students have misconceptions regarding various engineering disciplines.
- (B) Men with advanced degrees in mechanical engineering believe women are well suited to be mechanical engineers.
- (C) Mechanical engineering is a profession well suited for women with masters or higher degrees in mechanical engineering.
- (D) The number of women pursuing higher degrees in mechanical engineering is small.

8. Sourya committee had proposed the establishment of Sourya Institutes of Technology (SITs) in line with Indian Institutes of Technology (IITs) to cater to the technological and industrial needs of a developing country.

Which of the following can be logically inferred from the above sentence?

Based on the proposal,

- In the initial years, SIT students will get degrees from IIT.
- SITs will have a distinct national objective.
- SIT like institutions can only be established in consultation with IIT.
- SITs will serve technological needs of a developing country.

- (A) (iii) and (iv) only.
 (B) (i) and (iv) only.
 (C) (ii) and (iv) only.
 (D) (ii) and (iii) only.

9. Shaquille O' Neal is a 60% career free throw shooter, meaning that he successfully makes 60 free throws out of 100 attempts on average. What is the probability that he will successfully make exactly 6 free throws in 10 attempts

- (A) 0.2508 (B) 0.2816
 (C) 0.2934 (D) 0.6000

10. The numeral in the units position of $211^{870} + 146^{127} \times 3^{424}$ is _____.

SECTION II : Aerospace Engg.

Q. 1 – Q. 25 carry one mark each.

1. With increase in airfoil thickness, the critical Mach number for an airfoil is likely to
- (A) decrease. (B) increase.
 (C) remain unchanged. (D) be undefined.

2. Due to a body in potential flow, the velocity at a point A in the flow field is 20 m/s while the freestream velocity is only 10 m/s. The value of coefficient of pressure (C_p) at the point A is _____.

3. Which of the following airfoil will have location of the maximum camber at half chord length from the leading edge?
- (A) NACA 5212 (B) NACA 1225
 (C) NACA 2215 (D) NACA 2512

4. For a laminar incompressible flow past a flat plate at zero angle of attack, the variation of skin friction drag coefficient (C_f) with Reynolds number based on the chord length (Re_c) can be expressed as

- (A) $C_f \propto \sqrt{Re_c}$ (B) $C_f \propto Re_c$
 (C) $C_f \propto 1/\sqrt{Re_c}$ (D) $C_f \propto 1/Re_c$

5. Which of the following statement is NOT TRUE across an oblique shock wave?

- (A) Static temperature increases, total temperature remains constant.
 (B) Static pressure increases, static temperature increases.
 (C) Static temperature increases, total pressure decreases.
 (D) Static pressure increases, total temperature decreases.

6. For a completely subsonic isentropic flow through a convergent nozzle, which of the following statement is TRUE?

- (A) Pressure at the nozzle exit > back pressure.
 (B) Pressure at the nozzle exit < back pressure.
 (C) Pressure at the nozzle exit = back pressure.
 (D) Pressure at the nozzle exit = total pressure.

7. Which of the following aircraft engines has the highest propulsive efficiency at a cruising Mach number of less than 0.5?

- (A) Turbofan engine (B) Turbojet engine
 (C) Turboprop engine (D) Ramjet engine

8. Air, with a Prandtl number of 0.7, flows over a flat plate at a high Reynolds number. Which of the following statement is TRUE?

- (A) Thermal boundary layer is thicker than the velocity boundary layer.
 (B) Thermal boundary layer is thinner than the velocity boundary layer.
 (C) Thermal boundary layer is as thick as the velocity boundary layer.
 (D) There is no relationship between the thicknesses of thermal and velocity boundary layers.

9. Consider an eigenvalue problem given by $Ax = \lambda_i x$. If λ_i represent the eigenvalues of the non-singular square matrix A, then what will be the eigenvalues of matrix A^2 ?

- (A) λ_i^4 (B) λ_i^2
 (C) $\lambda_i^{1/2}$ (D) $\lambda_i^{1/4}$

10. If A and B are both non-singular $n \times n$ matrices, then which of the following statement is NOT TRUE. Note: det represents the determinant of a matrix.

- (A) $\det(AB) = \det(A)\det(B)$
 (B) $\det(A+B) = \det(A) + \det(B)$
 (C) $\det(AA^{-1}) = 1$
 (D) $\det(A^T) = \det(A)$

11. The total number of material constants that are necessary and sufficient to describe the three dimensional Hooke's law for an isotropic material is _____.

Q. 26 – Q. 55 carry two marks each.

26. An un-mixed turbofan engine with a bypass ratio of 6.0, flies with a velocity of 200 m/s. The core and the bypass nozzles of the engine, that are both convergent nozzles, operate under choked condition and have exhaust static temperatures of 580 K and 295 K, respectively. The specific gas constant and the ratio of specific heats for both the streams are 287 J/kgK and 1.4, respectively. If the fuel-air ratio is negligible, the thrust per unit mass flow rate generated by the engine is _____ Ns/kg.

27. A single-stage gas turbine operates with an axial absolute flow at the entry and exit from the stage. The absolute flow angle at the nozzle exit is 70°. The turbine stage generates a specific work of 228 kJ/kg when operating with a mean blade speed of 440 m/s. The absolute velocity at the rotor entry is
 (A) 275.7 m/s (B) 551.5 m/s
 (C) 1103.0 m/s (D) 1654.5 m/s

28. An axial compressor operates such that it has an inlet and an exit total temperature of 300 K and 430 K, respectively. The isentropic efficiency of the compressor is 85 %. If the ratio of specific heats is 1.4, then the total pressure ratio across the compressor is _____.

29. The maximum value of coefficient of lift (C_l) for a 2D circular cylinder, provided at least one stagnation point lies on the cylinder surface, is predicted by the potential flow theory to be
 (A) $\pi/2$ (B) π
 (C) 2π (D) 4π

30. The nozzle AB leading to the test section of a low speed subsonic wind tunnel, has a contraction ratio of 10:1. The pressure difference across the nozzle is maintained at 1000 N/m² and the density of air is 1.23 kg/m³. Assuming one-dimensional, steady, inviscid flow, the velocity in the test section as measured at point B is _____ m/s.

31. The rate of change of moment coefficient with respect to the angle of attack, $\frac{\partial C_m}{\partial \alpha}$, at half chord point of a thin airfoil, as per approximations from the thin airfoil theory is
 (A) $\pi/4$ radian⁻¹ (B) $\pi/2$ radian⁻¹
 (C) π radian⁻¹ (D) 2π radian⁻¹

32. An untwisted wing of elliptic planform and aspect ratio 6 consists of thin symmetric airfoil sections. The coefficient of lift (C_L) at 10° angle of attack assuming inviscid incompressible flow is
 (A) $\pi^2/16$ (B) $\pi^2/12$
 (C) $\pi^2/8$ (D) $\pi/2$

33. A gaseous mixture of air and fuel enters a constant area combustion chamber at a velocity of 100 m/s and at a static temperature of 300 K. The heat release due to combustion is 1000 kJ/kg. The specific heat at constant pressure of the calorically perfect gas is 1000 J/kgK. The total temperature of air-fuel mixture after combustion is _____ K.

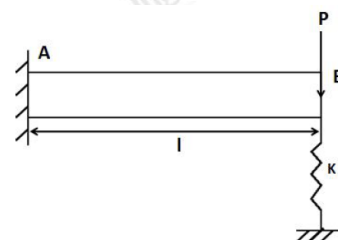
34. Consider 1-D, steady, inviscid, compressible flow through a convergent nozzle. The total temperature and total pressure are T_0, P_0 respectively. The flow through the nozzle is choked with a mass flow rate of \dot{m}_0 . If the total temperature is increased to $4T_0$, with total pressure remaining unchanged, then the mass flow rate through the nozzle
 (A) remains unchanged.
 (B) becomes half of \dot{m}_0
 (C) becomes twice of \dot{m}_0
 (D) becomes four times of \dot{m}_0

35. Consider a second order linear ordinary differential equation $\frac{d^2y}{dx^2} - 4\frac{dy}{dx} + 4y = 0$, with the boundary conditions $y(0) = 1; \frac{dy}{dx}|_{x=0} = 1$. The value of y at $x=1$ is
 (A) 0 (B) 1
 (C) e (D) e²

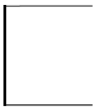
36. Consider the following system of linear equations:
 $2x - y + z = 1$
 $3x - 3y + 4z = 6$
 $x - 2y + 3z = 4$
 This system of linear equations has
 (A) no solution. (B) one solution.
 (C) two solutions. (D) three solutions.

37. A bar made of linear elastic isotropic material is fixed at one end and subjected to an axial force of 1 kN at the other end. The cross-sectional area of the bar is 100 mm², length is 100 mm and the Young's Modulus is 1×10^5 N/mm². The strain energy stored in the bar is _____ Nmm.

38. A cantilever beam-spring system is shown in the figure. The beam is made with a material of Young's modulus 1×10^5 N/mm² and geometry such that its moment of inertia is 100 mm⁴ and length $l = 100$ mm. It is supported by a spring of stiffness $K = 30$ N/mm and subjected to a load of $P = 100$ N at the point 'B'. The deflection at the point 'B' due to the load P is _____ mm.



39. Determine the correctness or otherwise of the following statements, [a] and [r],
 [a]: Ribs, used in airplane wings, increase the column buckling strength of the longitudinal stiffeners.
 [r]: Ribs distribute concentrated loads into the structure and redistribute stresses around discontinuities.
 (A) Both [a] and [r] are true and [r] is the correct reason for [a]
 (B) Both [a] and [r] are true but [r] is not the correct reason for [a]
 (C) Both [a] and [r] are false
 (D) [a] is true but [r] is false

40. A channel section shown in the figure has uniform thickness and each arm has a length 100 mm. It is subjected to an anticlockwise torque of 62.5×10^3 N-mm. The maximum possible thickness of the channel section, such that the shear stress induced in it does not exceed 100 N/mm^2 , is _____ mm.
- 

41. The governing differential equation of motion of a damped system is given by $m \frac{d^2x}{dt^2} + c \frac{dx}{dt} + kx = 0$. If $m = 1 \text{ kg}$, $c = 2 \text{ Ns/m}$ and $k = 2 \text{ N/m}$ then the frequency of the damped oscillation of this system is _____ rad/s.

42. The two dimensional state of stress in a body is described by the Airy's stress function:

$$\phi = 5 \frac{x^4}{12} + \frac{x^3y}{6} + 3 \frac{x^2y^2}{2} + 7 \frac{xy^3}{6} + E \frac{y^4}{12}$$

The Airy's stress function will satisfy the equilibrium and the compatibility requirements if and only if the value of the coefficient E is _____.

43. The value of definite integral $\int_0^\pi x \sin x dx$ is _____.

44. Use Newton-Raphson method to solve the equation: $xe^x = 1$. Begin with the initial guess $x_0 = 0.5$. The solution after one step is $x =$ _____.

45. A wall of thickness 5 mm is heated by a hot gas flowing along the wall. The gas is at a temperature of 3000 K, and the convective heat transfer coefficient is $160 \text{ W/m}^2\text{K}$. The wall thermal conductivity is 40 W/mK . If the colder side of the wall is held at 500 K, the temperature of the side exposed to the hot gas is _____ K.

46. A launch vehicle has a main rocket engine with two identical strap-on motors, all of which fire simultaneously during the operation. The main engine delivers a thrust of 6300 kN with a specific impulse of 428 s. Each strap-on motor delivers a thrust of 12000 kN with specific impulse of 292 s. The acceleration due to gravity is 9.81 m/s^2 . The effective (combined) specific impulse of the vehicle is _____ s.

47. A substance experiences an entropy change of $\Delta s > 0$ in a quasi-steady process. The rise in temperature (corresponding to the entropy change Δs) is highest for the following process:

- (A) isenthalpic (B) isobaric
 (C) isochoric (D) isothermal

48. In a particular rocket engine, helium propellant is heated to 6000 K and 95% of its total enthalpy is recovered as kinetic energy of the nozzle exhaust. Consider helium to be a calorically perfect gas with specific heat at constant pressure of 5200 J/kgK . The exhaust velocity for such a rocket for an optimum expansion is _____ m/s.

49. An aircraft is flying level in the North direction at a velocity of 55 m/s under cross wind from East to West of 5 m/s. For the given aircraft $C_{n\beta} = 0.012/\text{deg}$ and $C_{n\delta r} = -0.0072/\text{deg}$, where δ_r is the rudder deflection and β is the side slip angle. The rudder deflection exerted by pilot is _____ degrees.

50. An aircraft weighing 10000 N is flying level at 100 m/s and it is powered by a jet engine. The thrust required for level flight is 1000 N. The maximum possible thrust produced by the jet engine is 5000 N. The minimum time required to climb 1000 m, when flight speed is 100 m/s, is _____ s.

51. The aircraft velocity (m/s) components in body axes are given as $[u, v, w] = [100, 10, 10]$. The air velocity (m/s), angle of attack (deg) and sideslip angle (deg) in that order are

- (A) [120, 0.1, 0.1] (B) [100, 0.1, 0.1]
 (C) [100.995, 0.1, 5.73] (D) [100.995, 5.71, 5.68]

52. The Dutch roll motion of the aircraft is described by following relationship

$$\begin{bmatrix} \Delta\beta \\ \Delta\dot{r} \end{bmatrix} = \begin{bmatrix} -0.26 & -1 \\ 4.49 & -0.76 \end{bmatrix} \begin{bmatrix} \Delta\beta \\ \Delta\dot{r} \end{bmatrix}$$

The undamped natural frequency (rad/s) and damping ratio for the Dutch roll motion in that order are:

- (A) 4.68, 1.02 (B) 4.49, 1.02
 (C) 2.165, 0.235 (D) 2.165, 1.02

53. A glider weighing 3300 N is flying at 1000 m above sea level. The wing area is 14.1 m^2 and the air density is 1.23 kg/m^3 . Under zero wind conditions, the velocity for maximum range is _____ m/s.

α (deg)	C_L	C_D	C_L/C_D
11	1.46	0.0865	16.9
9	1.36	0.0675	20.1
7	1.23	0.0535	22.9
5	1.08	0.0440	24.5
3	0.90	0.0350	25.7
1	0.70	0.0275	25.4
-1	0.49	0.0220	22.2
-3	0.25	0.0180	13.8

54. A rocket, with a total lift-off mass of 10000 kg, moves vertically upward from rest under a constant gravitational acceleration of 9.81 m/s^2 . The propellant mass of 8400 kg burns at a constant rate of 1200 kg/s. If the specific impulse of the rocket engine is 240 s, neglecting drag, the burnout velocity in m/s is

- (A) 3933.7 (B) 4314.6
(C) 4245.9 (D) 4383.3

55. A satellite is injected at an altitude of 350 km above the Earth's surface, with a velocity of 8.0 km/s parallel to the local horizon. (Earth radius=6378 km, μ_E (GM=Gravitational constant \times Earth mass) = $3.986 \times 10^{14} \text{ m}^3\text{s}^{-2}$). The satellite

- (A) forms a circular orbit.
(B) forms an elliptic orbit.
(C) escapes from Earth's gravitational field.
(D) falls back to earth.

END OF THE QUESTION PAPER